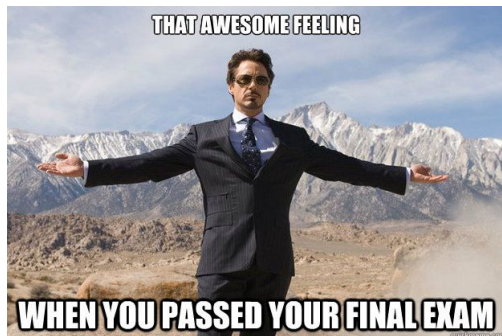


Outline

- 1 Review session: First order
- 2 Review session: Autonomous
- 3 Review session: Second order



Consider the equation

$$ty' + (t + 1)y = 2te^{-t}, y(1) = a, 0 < t \text{ as } t \rightarrow 0.$$

Determine the asymptotic behavior.

Homogeneous

Consider the equation

$$\frac{dy}{dx} = \frac{4y - 3x}{2x - y}.$$

Do change of variables $\nu(x) := y/x$ and find the implicit solution for $y(x)$.

Consider the equation

$$(x + 2)\sin(y) + x\cos(y)y' = 0.$$

Make it exact by checking the ratios from the formula sheet. Find the implicit solution.

Find that the lines perpendicular to

$$x^2 + y^2 = kx$$

using the perpendicular line equation $F_y dx - F_x dy = 0$. To make it exact multiply both sides by $x^m y^n$ and pick n, m to make it exact.

Consider the equation

$$\frac{dy}{dx} = y(1 - y^2).$$

Find the critical points, draw the phase line, and determine whether each critical point is asymptotically stable or unstable.

Consider the equation

$$\frac{dy}{dx} = e^{-y} - 2.$$

Find the critical point/s, draw the phase line, and determine whether each critical point is asymptotically stable or unstable.

Consider the equation

$$y'' - 2y' - 3y = -3te^{-t} + 2e^{-t}.$$

What does the stability criterion tell you? Solve and obtain asymptotic behaviour.

For $f(t) = ct^m e^{r_* t}$ the ansatz is

$$y_{nh} = t^s e^{r_* t} (a_0 + a_1 t + \dots + a_m t^m).$$

For $f(t) = ct^m e^{\alpha t} \cos(\beta t)$ or $= ct^m e^{\alpha t} \sin(\beta t)$ the ansatz is

$$y_{nh} = t^s e^{\alpha t} [(a_0 + a_1 t + \dots + a_m t^m) \cos(\beta t) + (b_0 + b_1 t + \dots + b_m t^m) \sin(\beta t)].$$

Consider the equation

$$y'' + 2y' + y = -3te^{-t} + 2e^{-t}$$

What does the stability criterion tell you? Solve and obtain asymptotic behaviour.

For $f(t) = ct^m e^{r_* t}$ the ansatz is

$$y_{nh} = t^s e^{r_* t} (a_0 + a_1 t + \dots + a_m t^m).$$

For $f(t) = ct^m e^{\alpha t} \cos(\beta t)$ or $= ct^m e^{\alpha t} \sin(\beta t)$ the ansatz is

$$y_{nh} = t^s e^{\alpha t} [(a_0 + a_1 t + \dots + a_m t^m) \cos(\beta t) + (b_0 + b_1 t + \dots + b_m t^m) \sin(\beta t)].$$

Consider the equation

$$y'' - 2y' - 3y = 3\sin(t).$$

What does the stability criterion tell you? Solve and obtain asymptotic behaviour.

For $f(t) = ct^m e^{r_* t}$ the ansatz is

$$y_{nh} = t^s e^{r_* t} (a_0 + a_1 t + \dots + a_m t^m).$$

For $f(t) = ct^m e^{\alpha t} \cos(\beta t)$ or $= ct^m e^{\alpha t} \sin(\beta t)$ the ansatz is

$$y_{nh} = t^s e^{\alpha t} [(a_0 + a_1 t + \dots + a_m t^m) \cos(\beta t) + (b_0 + b_1 t + \dots + b_m t^m) \sin(\beta t)].$$

Consider the equation

$$y'' + y = 3\sin(t).$$

What does the stability criterion tell you? Solve and obtain asymptotic behaviour.

For $f(t) = ct^m e^{r_* t}$ the ansatz is

$$y_{nh} = t^s e^{r_* t} (a_0 + a_1 t + \dots + a_m t^m).$$

For $f(t) = ct^m e^{\alpha t} \cos(\beta t)$ or $= ct^m e^{\alpha t} \sin(\beta t)$ the ansatz is

$$y_{nh} = t^s e^{\alpha t} [(a_0 + a_1 t + \dots + a_m t^m) \cos(\beta t) + (b_0 + b_1 t + \dots + b_m t^m) \sin(\beta t)].$$

Consider the equation

$$y'' + y = 3\sin(t) + t\cos(2t).$$

What does the stability criterion tell you? Solve and obtain asymptotic behaviour.

For $f(t) = ct^m e^{r_* t}$ the ansatz is

$$y_{nh} = t^s e^{r_* t} (a_0 + a_1 t + \dots + a_m t^m).$$

For $f(t) = ct^m e^{\alpha t} \cos(\beta t)$ or $= ct^m e^{\alpha t} \sin(\beta t)$ the ansatz is

$$y_{nh} = t^s e^{\alpha t} [(a_0 + a_1 t + \dots + a_m t^m) \cos(\beta t) + (b_0 + b_1 t + \dots + b_m t^m) \sin(\beta t)].$$

The End