# EMPIRICAL INDUSTRIAL ORGANIZATION (ECO 310) 

Fall 2022 - Victor Aguirregabiria

## PROBLEM SET 2

Due on Sunday, November 20, before 11:59pm via Quercus

INSTRUCTIONS. Please, follow these instructions for the submission of your completed problem set.

1. Write your answers electronically in a word processor.
2. For the answers that involve coding in STATA, include in the document the code in STATA that you have used to obtain your empirical results.
3. Convert the document to PDF format.
4. Submit your problem set in PDF online via Quercus.
5. You should submit your completed problem set by Sunday, November 20, 11:59pm.
6. You can discuss about the problem set with you classmates, but your answers and code should be written individually.

The total number of marks is 200.

To answer the Questions in this Problem Set, you need to use the datafile datafile_problemset_02_2022.dta that you can download from the course website in Quercus. Use this dataset to implement the estimations described below. Please, provide the STATA code that you use to obtain the results.

This dataset contains information on the retail wine industry in a Canadian province. It is a panel dataset with three dimensions: wine product, retail store, and month. It includes 11,033 wine products, 623 stores, and 12 months, and a total of $6,180,915$ product-store-month observations.

The following Table provides a brief description of all the variables in this dataset.

|  | Description of datafile <br> datafile_problemset_02_2022.dta |
| ---: | :--- |
| Variable name | Description |
| product | Wine Product ID Number |
| store | Store ID Number |
| period | Month count: from 1 to 12 |
| qunit | Quantity (750ml bottles) sold of product in store and month |
| price_750ml | Price of Product per 750ml bottle |
| alc | Alcohol percentage points of Wine Product |
| sugar_gpl | Sugar (gram per litter) of Wine Product |
| redwine | Dummy for Red Wine |
| whitewine | Dummy for White Wine |
| num_country | Country of origin of Wine Product |
| ontario | Dummy for Ontario origin of Wine Product |
| winerack | Dummy for Wine Product belongs Wine Rack Brand |
| wineshop | Dummy for Wine Product belongs Wine Shop Brand |
| otherontario | Dummy for Ontario Wine other than Wine Rack or Wine Shop |
| local_msize | Market size (in bottles of wine) at store-month |
|  |  |

For the rest of this problem set, we use the following subindexes: $j$ for product, $m$ for store (local market), and $t$ for month.

Consider the following Logit Demand Model:

$$
\begin{equation*}
\ln \left(\frac{s_{j m t}}{s_{0 m t}}\right)=-\alpha p_{j t}+\mathbf{x}_{j} \boldsymbol{\beta}+\xi_{j m t} \tag{1}
\end{equation*}
$$

Variable $s_{j m t}$ is the market share of product $j$ in store $m$ and month $t$, that is, $s_{j m t}=$ $\frac{\text { qunit }}{\text { localmsize. }}$. Variable $p_{j t}$ represents the price of product $j$ at month $t$, that is, $p_{j t}=$ price 750 ml . Note that, in this province, the price of a product is the same across all the local markets (stores). Finally, vector $\mathbf{x}_{j}$ contains the following product characteristics:
$\mathbf{x}_{j}=($ alc, sugargpl, redwine, whitewine, winerack, wineshop, otherontario, Country dummies)

QUESTION 1. [20 points]. (A) Construct market shares $s_{j m t}$ and $s_{0 m t}$, and variable $y_{j m t}=$ $\ln \left(s_{j m t} / s_{0 m t}\right)$. (B) Present a figure with the histogram of $y$.

QUESTION 2. [20 points]. Obtain the OLS estimates of parameters $\alpha$ and $\beta$ in equation (1). In this regression, include store fixed effects and month fixed effects. When reporting your table of estimation results, please do not include estimated coefficients for store dummies and month dummies.

QUESTION 3. [20 points]. Based on your estimates in Question 2, provide an estimate of the willingness to pay (in dollars per 750 ml bottle) of the average consumer for the following changes.
a. A reduction in alcohol content of 1 percent point.
b. An increase in sugar content of 1 gram per liter.
c. Switching from a white wine to a read wine.
d. Switching from "otherontario" wine to "wineshop" wine.
e. Switching from a French wine to a Canadian wine.

QUESTION 4. [10 points]. Based on the estimates in Question 2, obtain a variable with the estimated own-price demand elasticity $-\frac{d s_{j m t}}{d p_{j m t}} s_{j m t}$ for every observation $(j, m, t)$ in the data. Present the mean and median of this variable, and a figure with its histogram.

QUESTION 5. [20 points]. Suppose that $\xi_{j m t}$ follows an $\operatorname{AR}(1)$ process: $\xi_{j m t}=\rho \xi_{j m, t-1}+$ $a_{j m t}$. Obtain the OLS Cochrane-Orcutt estimates of parameters $\rho, \alpha, \rho \alpha$, and $(1-\rho) \beta$. In this regression, include store fixed effects and month fixed effects. Do not report coefficients for store dummies and month dummies.

QUESTION 6. [10 points]. Based on the estimates in Question 5, obtain a variable with the estimated own-price demand elasticity $-\frac{d s_{j m t}}{d p_{j m t}} \frac{p_{j m t}}{s_{j m t}}$ for every observation $(j, m, t)$ in the data. Present the mean and median of this variable, and a figure with its histogram.

QUESTION 7. [10 points]. Taking into account potential endogeneity, interpret the different estimates of $\alpha$ and of the corresponding demand elasticities in Questions 2 and 5. Based on this interpretation, select between one of these two demand estimations. Justify your choice.

For the remaining questions, we consider the following assumptions.
A. Each wine product is produced by a single manufacturer, and that each manufacturer produces only one wine product. Therefore, $j$ indexes both products and firms.
B. Firms (i.e., wine manufacturers) compete in prices a la Nash-Bertrand.
C. Each store $m$ is a separate geographic market where firms (i.e., wine manufacturers) compete with each other.
D. Every firm can choose a different for its wine product at each store.
E. The marginal cost of product $j$ in market $m$ at month $t, M C_{j m t}$, is constant: that is, $M C_{j m t}$ does not depend on the amount of output $q_{j m t}$.

## QUESTION 8. [10 points].

a. Obtain the expression for the first order condition of profit maximization for firm $j$ in market $m$ at month $t$.
b Based on this condition, obtain a "pricing equation" for price $p_{j m t}$ in terms of $M C_{j m t}$ and a price-cost margin term that depends only on $\alpha$ and $s_{j m t}$.
c. Define the price-cost margin $P C M_{j m t}$ as $\frac{p_{j m t}-M C_{j m t}}{p_{j m t}}$. Obtain an expression for the price-cost margin in terms only of $\alpha, s_{j m t}$, and $p_{j m t}$.

QUESTION 9. [20 points]. Use the expressions in Question 8 to obtain estimates of $M C_{j m t}$ and of $P C M_{j m t}$ for every observation $(j, m, t)$. Use your favorite estimate of $\alpha$. Obtain the mean and median of $P C M$. Present a histogram of the estimated $P C M s$.

For Question 10 below, take into account the equation for market share in a demand logit model:

$$
\begin{equation*}
s_{j m t}=\frac{a_{j m t} \exp \left\{-\alpha p_{j m t}+w_{j m t}\right\}}{1+\sum_{i=1}^{J} a_{i m t} \exp \left\{-\alpha p_{i m t}+w_{i m t}\right\}} \tag{2}
\end{equation*}
$$

where $a_{j m t} \in\{0,1\}$ is a binary variable that indicates whether product $j$ is available in store $m$ at month $t$. i.e., $a_{j m t}$ is the indicator of $q_{j m t}>0$. Variable $w_{j m t}$ is equal to $\mathbf{x}_{j} \boldsymbol{\beta}+$ $\xi_{j m t}$, and it can be interpreted as an index of product quality. Also, note that in the logit demand model, taking into account equation (1), we can obtain $w_{j m t}$ using the following equation:

$$
\begin{equation*}
w_{j m t}=\ln \left(\frac{s_{j m t}}{s_{0 m t}}\right)+\alpha p_{j t} \tag{3}
\end{equation*}
$$

QUESTION 10. [60 points]. Given your estimates of demand parameters and MCs, we are interested in evaluating the effects on quantities, prices, firms' profits, and consumer welfare of a hypothetical (counterfactual) increase in the tax of alcohol. Suppose that the tax increase is equal to 1 cent of a dollar per percentage of alcohol in the product, i.e., taxchange $_{j}=\$ 0.01 *$ alc $_{j}$.
a. [5 points] Calculate new variable taxchange with taxchange $_{j m t}$ for every observation $(j, m, t)$. Add taxchange to the estimated marginal cost to obtain the new (counterfactual) marginal cost for every observation $(j, m, t)$.
b. [5 points] Using equation (3), calculate a new variable wquality with $w_{j m t}$ for every observation $(j, m, t)$.
c. [20 points] Obtain an approximation to the new (counterfactual) equilibrium prices and market shares using the following iterative procedure.

Step 1. Use the pricing equation in Question $8(\mathrm{~b})$ to obtain new prices, say $p_{j m t}^{I T E R ~} 1$, using the new MCs, your estimate of $\alpha$, and $s_{j m t}$ in the data.
Step 2. Use equation (2) for market shares, your estimates for product qualities $w_{j m t}$, and new prices $p_{j m t}^{I T E R} 1$ to calculate new market shares, say $s_{j m t}^{I T E R} 1$.
Step 3. Similar as Step 1 but using market shares $s_{j m t}^{I T E R ~} 1$ instead of the shares in the data. Let $p_{j m t}^{I T E R ~} 2$ be the prices you obtain after applying this iteration.
Step 4. Similar to Step 2 but using prices $p_{j m t}^{I T E R} 2$ instead of $p_{j m t}^{I T E R 1}$. Let $s_{j m t}^{I T E R} 2$ be the shares you obtain after applying this iteration.
d. [30 points] Suppose that $p_{j m t}^{I T E R} 2$ and $s_{j m t}^{I T E R} 2$ are prices and market shares after the implementation of this counterfactual tax change. Calculate the following statistics at the aggregate annual and province level:

- Median price change.
- Change in annual sales of wine in this province.
- Government annual revenue from this tax increase.
- Change in total annual firms' profits in this province.
- Change in annual Consumer Surplus in this province.
- Annual Deadweight Loss of this tax: Change in consumer surplus + Change in firms' profits + Change in government revenue.

Interpret the results.
Hint to obtain the change in Consumer Surplus. You can approximate the change in consumer surplus applying the following formula for each observation $(j, m, t)$. Let ( $\left.p^{\text {data }}, q^{\text {data }}\right)$ be price and quantity in the data, and let $\left(p^{\operatorname{tax}}, q^{\operatorname{tax}}\right)$ be price and quantity after the tax. Define the change in price as $\Delta p \equiv p^{\operatorname{tax}}-p^{d a t a}$, and the change in quantity as $\Delta q \equiv q^{t a x}-q^{\text {data }}$. Then, the change in consumer surplus can be obtained using the following triangular approximation:

$$
\begin{equation*}
\Delta C S \equiv C S^{t a x}-C S^{\text {data }}=-\Delta p q^{t a x}+\frac{1}{2} \Delta p \Delta q \tag{4}
\end{equation*}
$$

