ECO 3901 EMPIRICAL INDUSTRIAL ORGANIZATION

Lecture 7
Dynamic Games of Innovation

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Dynamic Games of Innovation: Introduction

- We study the long lasting debate on the causal effect of competition on innovation, e.g.,
 - Schumpeter (1942): Increasing competition reduces the rents from innovation and then the incentive to innovate.
 - Arrow (1962): Monopoly power creates an incentive to protect the status quo and then a disincentive to further innovation.
- We examine recent applications of dynamic games of innovation.
- I will emphasize the following point: the sign and magnitude of the causal effect of competition on innovation depends crucially on the type of exogenous change generating variation in competition.
 - The effect is very different if the exogenous change is a merger, or increasing market size, or reduction in entry costs, etc.

Causal Effects of Competition on Innovation

- Let *RD* be a measure of innovation (e.g., R&D investment); let *PCM* be a measure of market power (e.g., price-cost markgin); and let *Z* be a exogenous variable affecting *RD* and *PCM* (e.g., market size, entry cost, number of potential entrants, etc).
- Both RD and PCM are endogenous in our models.
- Suppose that we measure the causal effect of RD on PCM using the following IV or LATE parameter:

$$\beta_Z = \frac{Cov(RD, Z)}{Cov(PCM, Z)}$$

- This LATE parameter β_Z has the standard causal interpretation.
- Our structural models show that the sign and magnitude of betaz
 depends critically on the exogenous variation Z used, e.g., a
 merger, increase in market size, policy change reducing entry cost, etc.

DYNAMIC GAMES OF FIRMS' INNOVATION: OUTLINE

1. **Vives (JIE, 2008):**

A systematic (static) theoretical analysis of the causal effect of competition on innovation.

2. **Igami (JPE, 2017):**

Creative destruction, cannibalization, and the incentives to innovate of incumbents and new entrants.

Gettler & Gordon (JPE, 2011):

Competition & innovation in CPU industry: Intel vs AMD.

Vives (JIE, 2008):
 Theoretical analysis
 of the causal effect
 of competition on innovation

Competition and Innovation: Vives (2008) [2]

- Vives considers a systematic theoretical analysis:
- [1] Different sources of exogenous increase in competition.
 - (i) reduction in entry cost; (ii) increase in market size; (iii) increase in degree of product substitutability.
- [2] Different types of innovation.
 - (i) process or cost-reduction innovation; (ii) product innovation / new products.
- [3] Different models of competition and specifications.
 - (i) Bertrand; (ii) Cournot
- [4] Specification of demand linear, CES, exponential, logit, nested logit.



Competition and Innovation: Vives (2008) [3]

- Vives shows that
 - The type of exogenous variation generating change competition
 - The type of innovation (process or product)

are key to determine a positive or a negative relationship between competition and innovation.

- However,
 - The form of competition (Bertrand or Cournot)
 - The specification of the demand system.

Do not affect sign of relationship between competition & innovation.

Vives (2008): Model

- Static model with symmetric firms, endogenous entry.
- Profit of firm *j*:

$$\pi_j = [p_j - c(z_j)] \ s \ d(p_j, p_{-j}, z_j, z_{-j}, n; \alpha) - z_j - F$$

- s = market size; n = number of firms (endogenous).
- $d(p_j, p_{-j}, z_j, z_{-j}, n; \alpha) = \text{demand per-consumer};$
- α = degree of substitutability;
- z_i = expenditure in cost reduction or product differentiation;
- $c(z_i) = \text{marginal cost (constant)}, c' < 0 \text{ and } c'' > 0$
- F = entry cost



Equilibrium

- Three-stage Nash equilibrium
 - Step 1: Market entry decisions.
 - Step 2: R&D investments z_j .
 - Step 3: Price (or quantity) competition.
- At stage 3: Marginal condition w.r.t cos-reduction R&D is:

$$-c'(z) s d(p, n; \alpha) -1 = 0$$

• Since c'' > 0, this implies

$$z = g(s d(p, n; \alpha))$$

where g(.) is an increasing function.

• The incentive to invest in cost reduction increases with output per firm, $q \equiv s \ d(p, n; \alpha)$.

Equilibrium (2)

• Any exogenous change in competition (say in α , s, or F) has three effects on output per firm and therefore on investment in cost-reduction R&D.

$$\frac{dz}{d\alpha} = g'(q) \left[\frac{\partial \left[s \ d(p, n; \alpha) \right]}{\partial \alpha} + \frac{\partial \left[s \ d(p, n; \alpha) \right]}{\partial p} \frac{\partial p}{\partial \alpha} + \frac{\partial \left[s \ d(p, n; \alpha) \right]}{\partial n} \frac{\partial n}{\partial \alpha} \right]$$

- $\frac{\partial \left[s \ d(p, n; \alpha)\right]}{\partial \alpha}$ is the direct demand effect,
- $\frac{\partial [s \ d(p, n; \alpha)]}{\partial p} \frac{\partial p}{\partial \alpha}$ is the price pressure effect.
- $\frac{\partial \left[s \ d(p, n; \alpha)\right]}{\partial n} \frac{\partial n}{\partial \alpha}$ is the number of entrants effect.
- The effects of different changes in competition on cost-reduction R&D can be explained in terms of these three effects.

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Summary of comparative statics

- (i) Increase in market size.
 - Increases per-firm expenditures in cost-reduction;
 - Effect on product innovation can be either positive or negative.
- (ii) Reduction in cost of market entry.
 - Reduces per-firm expenditures in cost-reduction innovation.
 - Increases product innovation.
- (iii) Increase in degree of product substitution.
 - Increases innovation in cost-reduction;
 - Production innovation may increase or decline.

Some limitations in this analysis

- The previous analysis is static, without uncertainty, with symmetric and single product firms.
- Therefore, the following factors that relate competition and innovation are absent from the analysis.
- 1. Preemptive motives.
- 2. Cannibalization of own products.
- 3. **Demand dynamics: durability. Endogenous obsolescence** generates incentives to product innovation.
- To study these factors, we need dynamic games with uncertainty, and asymmetric multi-product firms.



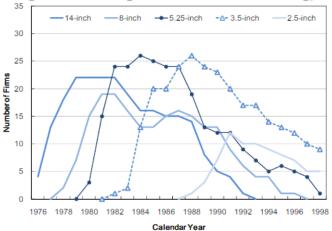
2. Creative destruction: incentives to innovate of incumbents and new entrants

Innovation and creative destruction (Igami, 2017)

- Innovation, the creation of new products and technologies, necessarily implies the "destruction" of existing products, technologies, and firms.
- The survival of existing products / technologies / firms is at the cost of preempting the birth of new ones.
- The speed of the innovation process in an industry depends on the dynamic strategic interactions between "old" and "new" products/technologies.
- Igami (JPE, 2017) studies these interactions in the context of the Hard-Disk-Drive (HDD) industry during 1981-1998.

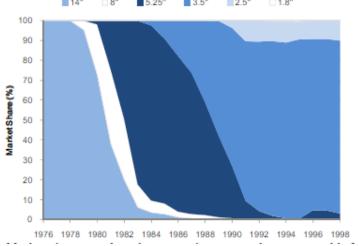
HDD: Different generations of products

Figure 2: Shifting Generations of Technology



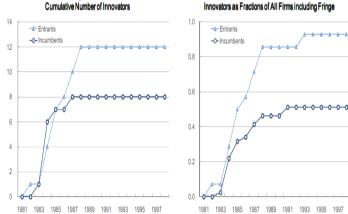
HDD: Different generations of products

Figure 12: Aggregate Market Share by Diameter



Adoption new tech: Incumbents vs. New Entrants

Figure 1: The Incumbent-Entrant Innovation Gap

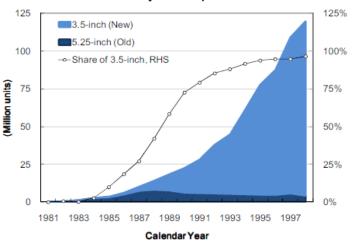


Adoption new tech: Incumbents vs. New Entrants (2)

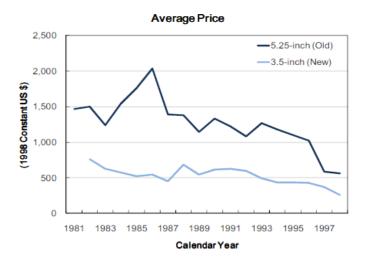
- Igami focuses on the transition from 5.25 to 3.5 inch products.
- He consider three main factors that contribute to the relative propensity to innovate of incumbents and potential entrants.
- Cannibalization. For incumbents, the introduction of a new product reduces the demand for their pre-existing products.
- Preemption. Early adoption by incumbents can deter entry and competition from potential new entrants.
- Differences in entry/innovation costs. It can play either way.
 Incumbents have knowledge capital and economies of scope, but they also have organizational inertia.

Market shares New/Old products

Industry-wide Shipment

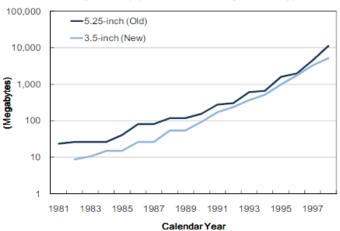


Average Prices: New/Old products



Average Quality: New/Old products

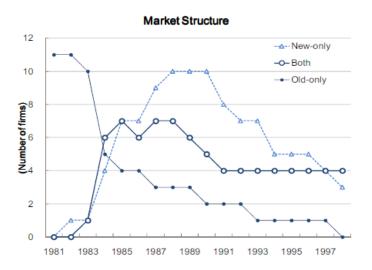
Average Quality (Information Storage Capacity)



Model

- Endogenous state var: s_{it} = products produced.
 - $s_{it} \in \{ potential entrant(pe); only old (old); only new (new); both$
- Market structure: $\{N_t^{pe}, N_t^{old}, N_t^{new}, N_t^{both}\}$.
- Timing within a period t:
 - 1. Incumbents compete (a la Cournot) ightarrow Period profits $\pi_t(s_{it}, s_{-it})$
 - 2. N_t^{old} firms simultaneously choose $a_{it}^{old} \in \{\textit{exit}, \textit{stay}, \textit{innovate}\}$
 - 3. N_t^{both} observe a_t^{old} and simul. choose $a_{it}^{both} \in \{\textit{exit}, \textit{stay}\}$
 - 4. N_t^{new} observe a_t^{old} , a_t^{both} and simul. choose $a_{it}^{new} \in \{exit, stay\}$
 - 5. N_t^{pe} observe a_t^{old} , a_t^{both} , a_t^{new} and simul. choose $a_{it}^{pe} \in \{entry, noentry\}$.

Market Structure: New/Old products



Model [2]

- Given these choices, next period market structure is obtained, s_{t+1} , and demand and cost variables evolve exogenously.
- Why imposing an order of move? This Assumption, together with:
 - Finite horizon T.
 - Homogeneous firms within type (up to i.i.d. private shocks). implies that there is a **unique Markov Perfect equilibrium**.
- This is very convenient for estimation (Igami uses a standard/Rust Nested Fixed Point Algorithm for estimation) and especially for counterfactuals.

Model: Demand

- Simple logit model of demand. A product is defined as a pair $\{\text{technology, quality}\}$, where $\text{technology} \in \{\textit{old, new}\}$ and quality(x) represents different storage sizes.
- Estimation:

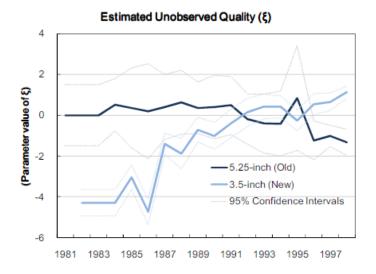
$$\ln\left(\frac{share_{jt}}{share_{0t}}\right) = \alpha_1 \ p_{jt} + \alpha_2 \ 1_j^{new} + \alpha_3 \ x_{jt} + \xi_{jt}$$

- Data: 72 quarters and 4 regions (broad market definition).
- IVs: Hausman-Nevo. Prices in other regions.

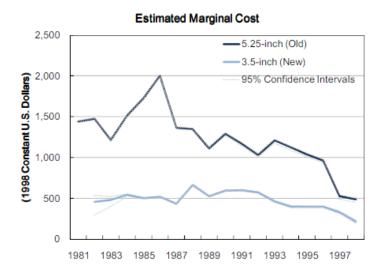
Estimates of Demand

Market definition:	Broad		Narrow	
Estimation method:	OLS	IV	OLS	IV
	(1)	(2)	(3)	(4)
Price (\$000)	-1.66***	-2.99***	93**	-3.28***
	(.45)	(.55)	(.46)	(.63)
Diameter = 3.5-inch	.84*	.75	1.75^{***}	.91**
	(.46)	(.45)	(.31)	(.38)
Log Capacity (MB)	.18	.87***	.04	1.20***
	(.33)	(.27)	(.26)	(.31)
Year dummies	Yes	Yes	Yes	Yes
Region/user dummies	_	_	Yes	Yes
Adjusted R^2	.43	.33	.50	.28
Number of obs.	176	176	405	405
Partial \mathbb{R}^2 for Price	_	.32	_	.16
P-value		.00		.00

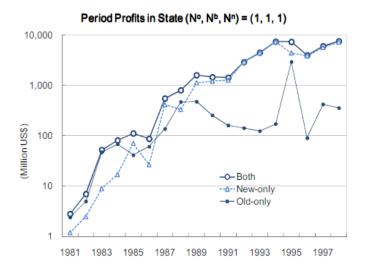
Evolution of unobserved Quality (epsi)



Evolution of Marginal Costs



Evolution of Period Profits [keeping market structure]



29 / 73

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Estimates of Dynamic Parameters

Table 4: Estimates of the Dynamic Parameters

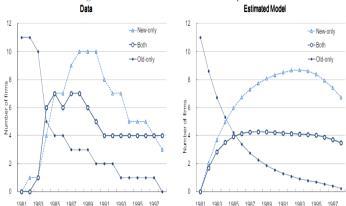
(\$ Billion)	Maximum Likelihood Estimates			
	(1)	(2)	(3)	
Assumed order of moves:	Old-Both-New-PE	PE-New-Both-Old	PE-Old-Both-New	
Fixed cost of operation (ϕ)	0.1474	0.1472	0.1451	
	$\begin{bmatrix} -0.02, & 0.33 \end{bmatrix}$	$\begin{bmatrix} -0.02, & 0.33 \end{bmatrix}$	[-0.03, 0.33]	
Incumbents' sunk cost (κ^{inc})	1.2439	1.2370	1.2483	
	[0.51, 2.11]	[0.50, 2.10]	0.51, 2.11	
Entrants' sunk cost (κ^{ent})	2.2538	2.2724	2.2911	
	[1.74, 2.85]	[1.76, 2.87]	[1.78, 2.89]	
Log likelihood	-112.80	-112.97	-113.46	

Estimates of Dynamic Parameters

- Estimates are pretty robust to changes in the order of move within a period.
- Cost for innovation is smaller for incumbents than for new entrants $(\kappa^{inc} < \kappa^{pe})$. Economies of scope seem more important than organizational inertia.
- Magnitude of entry costs are comparable to the annual R&D budget of specialized HDD manufacturers, e.g., Seagate Tech: between \$0.6B \$1.6B.

Estimated Model: Goodness of fit

Figure 5: Fit of Market Structure Dynamics



Counterfactuals

- Removing Cannibalization [two separate firms spinoff]
 - Substantial positive effect on incumbents' propensity to innovate.
 - Now incumbents (INC) have higher propensity to innovate than potential entrants (PE).
- Removing Preemption [Change INC's beliefs on PE's CCPs.
 INC believe PE's CCPs do not depend on INC's entry decision]
 - Reduces substantially the propensity to innovate of incumbents.
- Cannibalization is the main factor that explain the lower innovation propensity of incumbents. The strength of this effect more than offset the preemption motive and the lower entry cost of incumbents.

3. Competition and Innovation: Intel & AMD (Goettler & Gordon, 2011)

Introduction

- Competition between Intel & AMD in PC microprocessor industry.
- Incorporates product durability as a potentially important factor for innovation (endogenous technological obsolescence).
 - Most of the demand during 1993-2004 (> 89%) was upgrading.
- Two forces drive innovation (and relationship competition & innovation):
 - Quality competition between firms for the technological frontier.
 - Since PCs have little physical depreciation, firms have the incentive to innovate to **generate technological depreciation** of consumers' installed PCs that encourages them to upgrade.
- Duopolists face both forces, whereas a monopolist faces only the latter but in a stronger way (monopoly prices).

The PC microprocessor industry

- 1. Very **important to the economy**.
 - Computer equipment industry generated 25% of U.S. productivity growth in 1960-2007.
- 2. Interesting also from the point of view of **antitrust**.
 - In 2004, AMD sued Intel claiming anti-competitive practices:
 - * AMD's claim: Intel rewarded PC manufacturers that exclusively use Intel microprocessors (foreclosure).
 - In 2009, Intel settled these claims with \$1.25 B payment to AMD.
- 3. Quality and innovations are easy to measure.
 - Innovations in microprocessors are directly measured via improved performance on benchmark tasks. Most important: **CPU speed**.

The PC microprocessor industry (2)

- Market is a **duopoly**: AMD + Intel market shares = 95%
- Firms have high R&D intensities.
 - **R&D/Revenue ratios:** (1993-2004): AMD 20% ; Intel 11%
- Innovation is rapid: new products are released nearly every quarter.
- Gordon Moore's law: CPU speed doubles every 7 quarters.
- Positive spillovers: AMD and Intel extensively cross-license each other's technologies.

The PC microprocessor industry (3)

- Part of demand comes from the exogenous arrival of new (young) consumers to the market (first time PC buyers).
- A very important part of the demand comes from (old) consumers replacing / upgrading their PC/CPU

In 2004, 82% of PC purchases were replacements.

- Replacement is endogenous: speed of frontier microprocessors that encourages consumers to upgrade.
- Intertemporal Price Discrimination (IPD); Replacement cycles:
 - After introducing a new product, upgrading is slow because IPD.
 - Eventually, replacement demand drops and prices drop too (IPD).
 - Firms must release a new product to rebuild replacement demand.

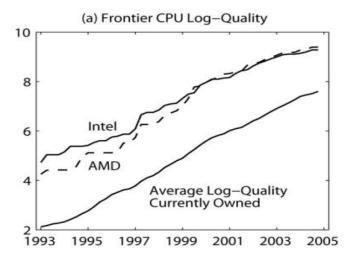
Data

- Proprietary data from a market research firm specializing in the microprocessor industry.
- Quarterly data from Q1-1993 to Q4-2004 (48 quarters).
- Information on:
 - Shipments in physical units for each type of CPU;
 - Manufacturers' average selling prices (ASP);
 - Production costs:
 - CPU characteristics (e.g., speed).
- All prices and costs are converted to base year 2000 dollars.
- Quarterly R&D investment levels, obtained from firms' annual reports.

Moore's Law

- Intel co-founder Gordon Moore predicted in 1965 that the number of transistors in a CPU (and therefore the CPU speed) would double every 2 years.
- Next slide shows "Moore's law" over the 48 quarters in the data.
- Quality is measured using processor speed.
- Quarterly % change in CPU speed: Intel = 10.2%; AMD = 11%.
- Note that there "plateaus" in evolution of frontier quality.

Moore's Law (Frontier CPU speed)

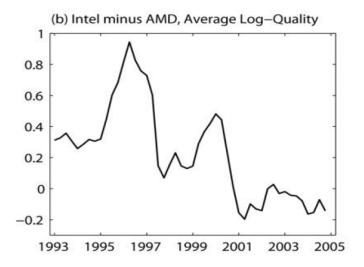




Differential log-quality between Intel and AMD

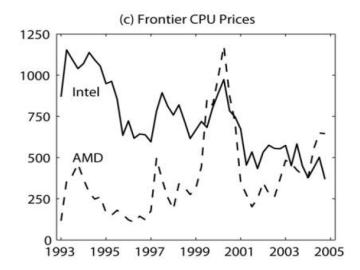
- Intel's initial quality advantage is moderate in 1993–94.
- Then, it becomes larger in 1995-96 when Intel releases the Pentium.
- AMD's responded in 1997 introducing the K6 processor that narrows the gap.
- But parity is not achieved until the mid-2000 when AMD released the Athlon.

Differential log-quality between Intel and AMD [2]

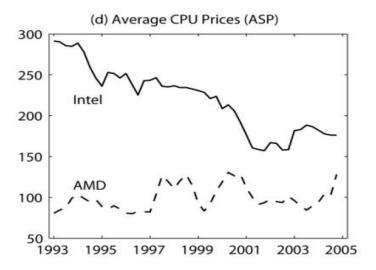




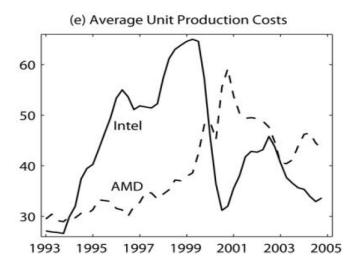
CPU Prices – Frontier Products



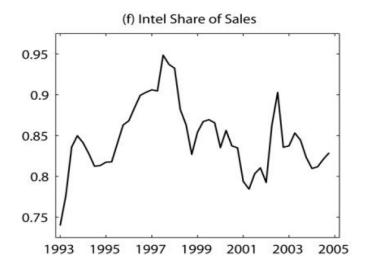
Average CPU Prices



Average Unit Production Costs



Intel Market Share



Model: General features

- Dynamic oligopoly with differentiated & durable products.
- Each firm sells a single product and invests in R&D to improve quality.
- q_{jt} = firm j's quality as measured by the logarithm of speed of the best product sold by this firm.

log quality:
$$q_{it} \in \{0, \delta, 2\delta, 3\delta, \dots\}$$

- If investment successful, $q_{j,t+1}=q_{jt}+\delta$; otherwise, $q_{j,t+1}=q_{jt}$.
- Consumers: Product durability. Utility of no-purchase choice is determined by quality of microprocessor consumer owns.

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Model: General features (2)

- ullet $\Delta_t = {\sf Distribution}$ of consumers according to owned quality, q^* .
 - $\Delta_t = [\# \text{ consumers with } q^* = 0; \# \text{ consumers with } q^* = \delta; ...]$
- $q^* = 0$ means consumer does not own a computer.
- In principle, the state space of Δ_t is unbounded and grows over time endogenously with technological progress.
- To bound this space, authors assume a maximum distance $c*\delta$ between q_t^* and frontier quality $q_t^{max} \equiv max\{q_{AMD,t},q_{Intel,t}\}$, such that:

$$q_t^* \in \{ \text{ 0, } q_t^{ extit{max}} - c \text{ } \delta, \text{ } q_t^{ extit{max}} - (c-1) \text{ } \delta, \text{ ..., } q_t^{ extit{max}} \}$$



Model: General features (3)

- Firms and consumers are forward looking.
- Consumer *i*'s state space consists of $(q_{it}^*, q_t, \Delta_t)$:
 - $q_{it}^* =$ Quality of her currently owned product;
 - $q_t = 2 \times 1$ vector of firms' current qualities;
 - Δ_t = distribution of consumers' owned qualities.
- Δ_t is part of the consumers' state space because it affects expectations on future prices.
- State space for firms is (q_t, Δ_t) .
- Given these state variables firms simultaneously choose prices p_{jt} and investment x_{it} .



Model: Consumer Demand

- Authors: "We restrict firms to selling only one product because the computational burden of allowing multiproduct firms is prohibitive".
- Consumers own no more than one microprocessor at a time. Utility for a consumer i from firm j's new product with quality q_{jt} is given by:

$$u_{ijt} = \gamma \ q_{jt} - \alpha \ p_{jt} + \xi_j + \varepsilon_{ijt}$$

Utility from the no-purchase option is:

$$u_{i0t} = \gamma \ q_{it}^* + \varepsilon_{i0t}$$

• A consumer maximizes her intertemporal utility given her beliefs about the evolution of future qualities and prices given (q_t, Δ_t) .

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Consumer Demand: Intertemporal Price Discrimination (IPD)

- The demand model does not incorporate ex-ante (persistent) heterogeneity in comsumers' preferences.
- Despite this, the model generates endogenously incentives for firms to use IPD.
- This is because consumers are "ex post" heterogeneous in owned q^* .
- Every period t, consumers with low q^* are willing to pay more for an upgrade.
- However, introducing persistent (ex-ante) heterogeneity in demand system would increase firms' inventive to IPD.



Model: Consumer Demand (3)

• Market shares for consumers currently owning q^* are:

$$s_{jt}(q^*) = \frac{\exp\{v_j(q_t, \Delta_t, q^*)\}}{\sum_{k \in \{0, Intel, AMD\}} \exp\{v_k(q_t, \Delta_t, q^*)\}}$$

• Using Δ_t to integrate over the distribution of q^* yields the market share of product j.

$$s_{jt} = \sum_{q^*} s_{jt}(q^*) \; \Delta_t(q^*)$$

• Transition rule of Δ_t . By definition, next period Δ_{t+1} is determined by a known closed-form function of Δ_t , q_t , and s_t .

$$\Delta_{t+1} = F_{\Delta}(\Delta_t, q_t, s_t)$$



Model: Firms' per period profits

The period profit function (not including investment costs) is:

$$\pi_j(p_t, q_t, \Delta_t) = M \ s_j(p_t, q_t, \Delta_t) \ [p_{jt} - mc_j(q_{jt})]$$

The specification of the marginal cost is:

$$\mathit{mc_j}(q_{jt}) = \lambda_{0j} - \lambda_1(q_t^{\mathsf{max}} - q_{jt})$$

• Parameter $\lambda_1 \geq 0$ captures that being in the frontier (i.e., $q_{jt} = q_t^{max}$) implies higher unit production costs. Or equivalently, marginal cost is smaller for the non-frontier firm.



Model: Firms' Innovation process

- Relationship between investment in R&D (x_{jt}) and log-quality improvement $(\Delta q_{jt+1} = q_{jt+1} q_{jt})$.
- Log-Quality improvement can take two values, 0 or δ .
- The probability that $\Delta q_{jt+1} = \delta$ is (Pakes & McGure, 1994):

$$\chi_j(x_{jt}, q_{jt}) = \frac{a_j(q_t) x_{jt}}{1 + a_j(q_t) x_{jt}}$$

where $a_j(q_t)$ is the "investment efficiency" function:

$$a_j(q_t) = a_{0,j} \max \left[1, a_1 \left(rac{q_t^{max} - q_{jt}}{\delta}
ight)^{1/2}
ight]$$

• It is decreasing in q_{jt} (i.e., $a_1 > 0$) to capture the idea of increasing difficulty of advancing the frontier relative to catching up.

Model: Firms' Bellman equation

• Let $W_j(q_t, \Delta_t)$ be the value function. The Bellman equation is:

$$W_{j}(q_{t}, \Delta_{t}) = \max_{x_{it}, p_{it}} \left[\pi_{j}(p_{t}, q_{t}, \Delta_{t}) - x_{jt} + \beta \mathbb{E}_{t} \left[W_{j}(q_{t+1}, \Delta_{t+1}) \right] \right]$$

 The decision variables are continuous, and the best response function should satisfy the F.O.C.

$$\frac{\partial \pi_{jt}}{\partial \rho_{jt}} + \beta \frac{\partial \mathbb{E}_{t} \left[W_{j,t+1} \right]}{\partial \rho_{jt}} = 0$$

$$\frac{\partial \pi_{jt}}{\partial x_{it}} - 1 + \beta \frac{\partial \mathbb{E}_{t} [W_{j,t+1}]}{\partial x_{it}} = 0$$



Model: Markov Perfect Equilibrium

- (1) firms' and consumers' equilibrium strategies depend only on current payoff relevant state variables (q_t, Δ_t) .
- (2) consumers have rational expectations about firms' policy functions.
- (3) each firm has rational expectations about competitors' policy functions and about the evolution of the ownership distribution.

Estimation

- Marginal cost parameters (λ_0, λ_1) are estimated in a first step because the dataset includes data on unit production costs.
- The rest of the structural parameters,

$$\theta = (\gamma, \ \alpha, \ \xi_{intel}, \ \xi_{amd}, \ a_{0,intel}, \ a_{0,amd}, \ a_{1})$$

- Demand: γ , α , ξ_{intel} , ξ_{amd} ; Investment innovation efficiency: $a_{0,intel}$, $a_{0,amd}$, a_{1} .
- θ is estimated using Indirect Inference or Simulated Method of Moments (SMM).

Estimation: Moments to match

- Mean of innovation rates $q_{j,t+1} q_{jt}$ for each firm.
- Mean R&D intensities x_{jt} / revenue_{jt} for each firm.
- Mean of differential quality $q_{intel,t} q_{amd,t}$, and share of quarters with $q_{intel,t} \ge q_{amd,t}$.
- Mean of gap $q_t^{\mathsf{max}} \overline{\Delta}_t$.
- Average prices, and OLS estimated coefficients of the regressions of p_{jt} on $q_{intel,t}$, $q_{amd,t}$, and average $\overline{\Delta}_t$.
- OLS estimated coefficients of the regression of s_{intel,t} on q_{intel,t} - q_{amd,t}.

Empirical and predicted moments

TABLE 1 Empirical and Simulated Moments

	Actual				
Moment	Actual	Standard Error	Fitted		
Intel price equation:					
Average Intel price	219.7	5.9	206.2		
$q_{\text{Intel},t} - q_{\text{AMD},t}$	47.4	17.6	27.3		
$q_{\mathrm{Intel},t} - \bar{\Delta}_t$	94.4	31.6	43.0		
AMD price equation:					
Average AMD price	100.4	2.3	122.9		
$q_{\text{Intel},t} = q_{\text{AMD},t}$	-8.7	11.5	-22.3		
$q_{\mathrm{AMD},t} - \bar{\Delta}_t$	16.6	15.4	5.9		
Intel share equation:					
Constant	.834	.007	.846		
$q_{\text{Intel},t} - q_{\text{AMD},t}$.055	.013	.092		
Potential upgrade gains:					
Mean $(\bar{q}_t - \hat{\Delta}_t)$	1.146	.056	1.100		
Mean innovation rates:					
Intel	.557	.047	.597		
AMD	.610	.079	.602		
Relative qualities:					
Mean $q_{\text{Intel},t} - q_{\text{AMD},t}$	1.257	.239	1.352		
Mean $\mathcal{I}(q_{\text{Intel},t} \ge q_{\text{AMD},t})$.833	.054	.929		
Mean R&D/revenue:					
Intel	.114	.004	.101		
AMD	.203	.009	.223		

Parameter estimates

TABLE 2 Parameter Estimates

Parameter	Estimate	Standard Error	
Price, α	.0131	.0017	
Quality, γ	.2764	.0298	
Intel fixed effect, ξ_{Intel}	6281	.0231	
AMD fixed effect, ξ_{AMD}	-3.1700	.0790	
Intel innovation, $a_{0,Intel}$.0010	.0002	
AMD innovation, $a_{0,AMD}$.0019	.0002	
Spillover, a_1	3.9373	.1453	
Stage 1 marginal cost equation:			
Constant, λ_0	44.5133	1.1113	
$\max(0, q_{\text{competitor},t} - q_{\text{own},t}), \lambda_1$	-19.6669	4.1591	

Parameter estimates (2)

- Demand: Dividing γ by α : consumers are willing to pay \$21 for enjoying during 1 quarter a $\delta=20\%$ increase in log quality.
- Dividing $\xi_{intel} \xi_{amd}$ by α : consumers are willing to pay \$194 for Intel over AMD.
- The model needs this strong brand effect to explain the fact that AMD's share never rises above 22 percent in the period during which AMD had a faster product.
- Intel and AMD's innovation efficiencies are estimated to be .0010 and .0019, respectively, as needed for AMD to occasionally be the technology leader while investing much less.

Counterfactuals: Industry Outcomes under Different Scenarios

TABLE 3 INDUSTRY OUTCOMES UNDER VARIOUS SCENARIOS

	AMD-INTEL Duopoly (1)	Symmetric Duopoly (2)	Monopoly (3)	No Spillover Duopoly (4)	Myopic Pricing	
					AMD-Intel (5)	Monopoly (6)
Industry profits (\$ billions)	408	400	567	382	318	322
Consumer surplus (CS)	2,978	3,012	2,857	3,068	2,800	2,762
CS as share of monopoly CS	1.042	1.054	1.000	1.074	.980	.967
Social surplus (SS)	3,386	3,412	3,424	3,450	3,118	3,084
SS as share of planner SS	.929	.906	.940	.916	.828	.819
Margins, $(p - mc)/mc$	3.434	2.424	5.672	3.478	2.176	2.216
Price	194.17	146.73	296.98	157.63	140.06	143.16
Frontier innovation rate	.599	.501	.624	.438	.447	.438
Industry investment (\$ millions)	830	652	1,672	486	456	787
Mean quality upgrade (%)	261	148	410	187	175	181
Intel or leader share	.164	.135	.143	.160	.203	.211
AMD or laggard share	.024	.125		.091	.016	

From current duopoly (1) to Intel Monopoly (3)

- Innovation rate increases from 0.599 to 0.624
- Mean quality upgrade increases 261% to 410%
- Investment in R&D: increases by 1.2B per quarter: more than doubles.
- Price increases in \$102 (70%)
- Consumer surplus declines in \$121M (4.2%)
- Industry profits increase in \$159M
- Social surplus increases in \$38M (less than 1%)

From current duopoly (1) to symmetric duopoly (2)

- Innovation rate declines from 0.599 to 0.501
- Mean quality declines from 261% to 148%
- Investment in R&D: declines by 178M per quarter
- Price declines in \$48 (24%)
- Consumer surplus increases in \$34M (1.2%)
- Industry profits decline in \$8M
- Social surplus increases in \$26M (less than 1%)

From current scenario (1) to myopic pricing

- It reduces prices, increases CS, and reduces firms' profits.
- Innovation rates and investment in R&D decline dramatically.
- Why? The higher induce firms to innovate more rapidly.
- Prices are higher with dynamic pricing because firms want to preserve future demand.

Counterfactuals

- The finding that innovation by a monopoly exceeds that of a duopoly reflects two features of the model:
 - the monopoly must innovate to induce consumers to upgrade;
 - the monopoly is able to extract much of the potential surplus from these upgrades because of its substantial pricing power.
- If there were a steady flow of new consumers into the market, such that most demand were not replacement, the monopoly would reduce innovation below that of the duopoly.

Counterfactuals: Foreclosure

- In 2009, Intel paid AMD \$1.25 billion to settle claims that Intel's anti-competitive practices foreclosed AMD from many consumers.
- To study the effect of such practices on innovation, prices, and welfare, the authors perform a series of counterfactual simulations in which they vary the portion of the market to which Intel has exclusive access.
- Let ζ be the proportion of foreclosure market. Intel market share becomes:

$$s_j^* = \zeta \ \widehat{s}_j + (1 - \zeta) \ s_j$$

where s_j is the market share when AMD is competing, and \hat{s}_j is the market share when Intel competes only with the outside alternative.

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Counterfactuals: Foreclosure (2)

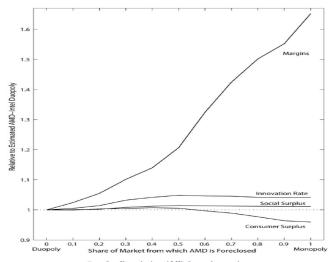


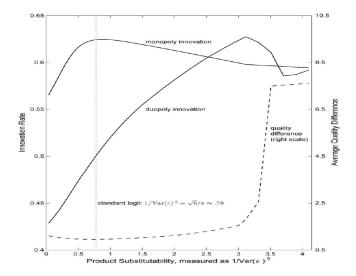
Fig. 6.—Foreclosing AMD from the market



Counterfactuals: Foreclosure (3)

- Margins monotonically rise steeply.
- Innovation exhibits an inverted U with a peak at $\zeta = 0.5$.
- Consumer surplus is actually higher when AMD is barred from a portion of the market, peaking at 40% foreclosure.
- This finding highlights the importance of accounting for innovation in antitrust policy:
 - Drop in consumer surplus from higher prices can be more than offset by the compounding effects of higher innovation rates.

Counterfactuals: Product Substitutability



Counterfactuals: Product substitutability (2)

- Innovation in the monopoly exhibits an inverted U as substitutability increases.
- Innovation in the duopoly increases as substitutability increases until Var() becomes too small for firms with similar qualities to coexist.
 - Beyond this "shakeout" threshold, the laggard eventually concedes the market as evidenced by the sharp increase in the quality difference.
- Duopoly innovation is higher than monopoly innovation when substitutability is near the shakeout threshold.

Summary of results

- The rate of innovation in product quality would be 4.2% higher if Intel were a monopolist, consistent with Schumpeter.
- Without AMD, higher margins spur Intel to innovate faster to generate upgrade sales.
- As in Coase's (1972) conjecture, product durability can limit welfare losses from market power.
- This result, however, depends on the degree of competition from past sales. If first-time purchasers were to arrive sufficiently faster, innovation in an Intel monopoly would be lower, not higher, since upgrade sales would be less important.