# ECO 310: Empirical Industrial Organization <br> Lecture 10: Models of Competition in Prices or Quantities: Conjectural Variations [2] 

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## Outline on today's lecture

1. Conjectural variations with product differentiation
2. Application (Homogeneous product): Genesove \& Mullin

## 2. Conjectural variations with product differentiation

## CVs with product differentiation

- I present this approach in a simplified model with 2 firms with 1 product each. It is straightforward to extend this approach to $N$ multiproduct firms (see Nevo (Econ Letters, 1998).
- Consider an industry with a differentiated product. Two firms: 1 and 2. Each firm produces and sells only one product.
- Profit of firm $i$ is:

$$
\Pi_{i}=p_{i} q_{i}-C_{i}\left(q_{i}\right)
$$

- Demand has a Logit structure:

$$
q_{1}=H s_{1}=\frac{\exp \left\{\beta x_{1}-\alpha p_{1}\right\}}{1+\exp \left\{\beta x_{1}-\alpha p_{1}\right\}+\exp \left\{\beta x_{2}-\alpha p_{2}\right\}}
$$

## Profit maximization

- Each firm $i$ chooses its own price $p_{i}$ to maximize its profit. The F.O.C of optimality for firm 1 is:

$$
\frac{d \Pi_{i}}{d p_{i}}=0 \Rightarrow q_{i}+p_{i} \frac{d q_{i}}{d p_{i}}-M C_{i} \frac{d q_{i}}{d p_{i}}=0
$$

- That we can write as:

$$
p_{i}-M C_{i}=\frac{-s_{i}}{\frac{d s_{i}}{d p_{i}}}
$$

- Now, we examine the term $\frac{d s_{i}}{d p_{i}}$ and how it depends on the Nature of Competition of Conjectural Variation (CV).


## Conjectural Variation

- Remember:

$$
s_{1}=\frac{\exp \left\{\beta x_{1}-\alpha p_{1}\right\}}{1+\exp \left\{\beta x_{1}-\alpha p_{1}\right\}+\exp \left\{\beta x_{2}-\alpha p_{2}\right\}}
$$

- Now, we have that $s_{1}$ depends on $p_{1}$ through two different channels:

$$
\left\{\begin{array}{l}
\text { Direct effect of } p_{1} \text { on } s_{1}  \tag{1}\\
\text { Indirect effect: } p_{1} \rightarrow p_{2} \rightarrow s_{1}
\end{array}\right.
$$

- Here we need to distinguish between total derivative $\frac{d s_{1}}{d p_{1}}$ and partial derivatives, $\frac{\partial s_{1}}{d p_{1}}$ and $\frac{\partial s_{1}}{d p_{2}}$. The partial derivative $\frac{\partial s_{1}}{d p_{1}}$ fixes $p_{2}$ as a constant, and the partial derivative $\frac{\partial s_{1}}{d p_{2}}$ fixes $p_{1}$ as a constant.


## Conjectural Variation

- We have:

$$
d s_{1}=\frac{\partial s_{1}}{\partial p_{1}} d p_{1}+\frac{\partial s_{1}}{\partial p_{2}} \frac{d p_{2}}{d p_{1}} d p_{1}
$$

- Or:

$$
\frac{d s_{1}}{d p_{1}}=\frac{\partial s_{1}}{\partial p_{1}}+\frac{\partial s_{1}}{\partial p_{2}} \frac{d p_{2}}{d p_{1}}
$$

- The term $\frac{d p_{2}}{d p_{1}}$ represents the Belief or Conjecture of firm 1 about the response of firm 2.
- We denote it as $C V_{1}$ (Firm 1's Conjectural Variation)


## Conjectural Variation

- For the standard Logit demand model: $\frac{\partial s_{1}}{\partial p_{1}}=-\alpha s_{1}\left(1-s_{1}\right)$ and $\frac{\partial s_{1}}{\partial p_{2}}=\alpha s_{1} s_{2}$, such that:

$$
\begin{aligned}
\frac{d s_{1}}{d p_{1}} & =\frac{\partial s_{1}}{\partial p_{1}}+\frac{\partial s_{2}}{\partial p_{1}} C V_{1} \\
& =-\alpha s_{1}\left(1-s_{1}\right)+\alpha s_{1} s_{2} C V_{1} \\
& =-\alpha s_{1}\left(1-s_{1}-s_{2} C V_{1}\right)
\end{aligned}
$$

- And plugging this into the F.O.C:

$$
p_{1}-M C_{1}=\frac{-s_{1}}{-\alpha s_{1}\left(1-s_{1}-s_{2} C V_{1}\right)}
$$

- Or:

$$
p_{1}-M C_{1}=\frac{1}{\alpha\left(1-s_{1}-s_{2} C V_{1}\right)}
$$

## Different Conjectures - Forms of Competition

- Nash-Bertrand competition: $C V_{1}=0$, such that:

$$
p_{1}-M C_{1}=\frac{1}{\alpha\left(1-s_{1}\right)}
$$

- Collusion between Firms 1 \& 2: $C V_{1}=1$, such that:

$$
p_{1}-M C_{1}=\frac{1}{\alpha\left(1-s_{1}-s_{2}\right)}
$$

- This expression corresponds to the F.O.C. of when firms $1 \& 2$ choose their prices as if they were a single firm maximizing their joint profits.


## Extension to N firms

- With $N>2$ firms, the $C V_{i \rightarrow j}$ represent firm i's conjecture about the response of firm $j: \frac{d p_{j}}{d p_{i}}$.
- Then, for the logit model we have that the F.O.C. of profit maximization for firm $i$ becomes:

$$
p_{i}-M C_{i}=\frac{1}{\alpha\left(1-s_{i}-\sum_{j \neq i} s_{j} C V_{i \rightarrow j}\right)}
$$

## Identification of Collusion

$$
p_{i}-M C_{i}=\frac{1}{\alpha\left(1-s_{i}-\sum_{j \neq i} s_{j} C V_{i \rightarrow j}\right)}
$$

- As in the homogeneous product case, we need to distinguish two cases: MC's known or unknown to the researcher.
- Empirical papers focus on the identification of collusion:

$$
\left\{\begin{array}{l}
C V_{i \rightarrow j} \text { is either } 0 \text { or } 1 \\
C V_{i \rightarrow j}=C V_{j \rightarrow i}
\end{array}\right.
$$

- This is identified under mild conditions.


## 2. Empirical application: <br> Genesove \& Mullin

## An Application: US sugar industry 1890-1914

- Genesove and Mullin (GM) study competition in the US sugar industry during the period 1890-1914.
- Why this period? High quality information on the value of marginal costs because:
(1) the production technology of refined sugar during this period was very simple;
(2) there was an important investigation of the industry by the US anti-trust authority. As a result of that investigation, there are multiple reports from expert witnesses that provide estimates about the structure and magnitude of production costs in this industry.


## The industry

- Homogeneous product industry.
- Highly concentrated during 1890-1914. The industry leader, American Sugar Refining Company (ASRC), had more than 65\% of the market share during most of these years.
- Refined sugar companies buy "raw sugar" from suppliers in national or international markets, transformed it into refined sugar, and sell it to grocers.
- Production technology.
- Raw sugar is $96 \%$ sucrose and $4 \%$ water. Refined sugar is $100 \%$ sucrose. Process of transforming raw sugar into refined sugar is called "melting".
- Industry experts reported that the industry is a "fixed coefficient" production technology


## Production technology: Costs

- "Fixed coefficient" production technology

$$
q^{\text {refined }}=\lambda q^{\text {raw }}
$$

where $q^{\text {refined }}$ is refined sugar output, $q^{\text {raw }}$ is the input of raw sugar, and $\lambda \in(0,1)$ is a technological parameter.

- Marginal cost function. Given this production technology, the marginal cost function is:

$$
M C=c_{0}+\frac{1}{\lambda} P^{r a w}
$$

- Praw is the price of the input raw sugar (in dollars per pound).
- $c_{0}$ is a component of the marginal cost that depends on labor and energy.


## Production technology: Costs

$$
M C=c_{0}+\frac{1}{\lambda} P^{r a w}
$$

- Industry experts unanimously report that the value of the parameter $\lambda$ was close to 0.93 , and $c_{0}$ was around $\$ 0.26$ per pound.
- Therefore, the marginal cost at period (quarter) $t$, in dollars per pound of sugar, was:

$$
M C_{t}=0.26+1.075 P_{t}^{\text {raw }}
$$

## Data

- Quarterly US data for the period 1890-1914.
- The dataset contains 97 quarterly observations on industry output, price, price of raw sugar, imports of raw sugar, and a seasonal dummy.

$$
\text { Data }=\left\{Q_{t}, P_{t}, P_{t}^{\text {raw }}, I M P_{t}, S_{t}: t=1,2, \ldots, 97\right\}
$$

- $I M P_{t}$ represents the imports of raw sugar from Cuba.
- And $S_{t}$ is a dummy variable for the Summer season: $S_{t}=1$ is observation $t$ is a Summer quarter, and $S_{t}=0$ otherwise.
- The summer was a high demand season for sugar because most the production of canned fruits was concentrated during that season, and the canned fruit industry accounted for an important fraction of the demand of sugar.


## Estimates of demand parameters

- GM estimate four different models of demand. The main results are consistent for the four models. Here I concentrate on the linear demand.

$$
Q_{t}=\beta_{t}^{D}\left(\alpha_{t}^{D}-P_{t}\right)
$$

- GM consider the following specification for $\alpha_{t}$ and $\beta_{t}$ :

$$
\begin{aligned}
& \alpha_{t}^{D}=\alpha_{L}^{D}\left(1-S_{t}\right)+\alpha_{H}^{D} S_{t}+e_{t}^{D} \\
& \beta_{t}^{D}=\beta_{L}^{D}\left(1-S_{t}\right)+\beta_{H}^{D} S_{t}
\end{aligned}
$$

- $\alpha_{L}^{D}$ and $\beta_{L}^{D}$ are the intercept and the slope of the demand during the "Low Season" (when $S_{t}=0$ ).
- And $\alpha_{H}^{D}$ and $\beta_{H}^{D}$ are the intercept and the slope of the demand during the "High Season" (when $S_{t}=1$ ).


## Estimates of demand parameters

| Demand Estimates |  |  |
| :--- | :--- | :--- |
| Parameter | Estimate | Standard Error |
| $\alpha_{L}^{D}$ | 5.81 | $(1.90)$ |
| $\alpha_{H}^{D}$ | 7.90 | $(1.57)$ |
| $\beta_{L}^{D}$ | 2.30 | $(0.48)$ |
| $\beta_{H}^{D}$ | 1.36 | $(0.36)$ |

- According to these estimates, in the high season the demand shifts upwards but it also becomes more inelastic.
- The estimated price elasticities of demand in the low and the high season are $\eta_{L}=2.24$ and $\eta_{H}=1.04$, respectively.
- According to this, any model of oligopoly competition where firms have some market power predicts that the price cost margin should


## Estimates of demand parameters

- Importantly, the seasonality in the demand of sugar introduces a "rotator" in the demand curve.
- The slope of the demand curve is steeper in the high season than in the low season.


## Estimates of CVs

- GM specify a constant-cost Marginal Cost function for US sugar producers

$$
M C_{t}=\beta_{0}^{M C}+\beta_{1}^{M C} P_{t}^{R A W}+\beta_{2}^{M C} q_{t}+\varepsilon_{t}^{M C}
$$

- The $M R=M C$ condition yields:

$$
P_{t}=\beta_{0}^{M C}+\beta_{1}^{M C} P_{t}^{R A W}+\gamma_{1} q_{t}+\gamma_{2}\left(S_{t} q_{t}\right)+\varepsilon_{i t}^{M C}
$$

where

$$
\begin{aligned}
& \gamma_{1}=\beta_{2}^{M C}+\frac{1}{\beta_{L}^{D}}[1+C V] \\
& \gamma_{2}=\left(\frac{1}{\beta_{H}^{D}}-\frac{1}{\beta_{L}^{D}}\right)[1+C V]
\end{aligned}
$$

## Estimation Results

|  | Estimate | Direct Measure |
| :---: | :---: | :---: |
| $C V / N$ | 0.038 | 0.100 |
|  | $(0.014)$ |  |
| $\beta_{0}^{M C}$ | 0.466 | 0.260 |
| $\beta_{1}^{M C}$ | $0.285)$ <br> 1.052 <br> $(0.085)$ | 1.075 |

- Estimated cost parameters not too far from their "direct measures" which seems to validate CV approach.
- Evidence of collusion

